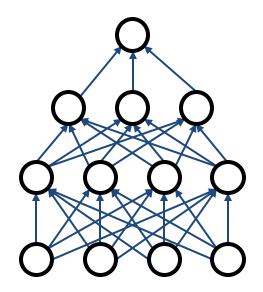
## **CS 4644-DL / 7643-A: LECTURE 12 DANFEI XU**

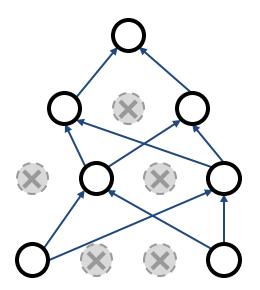
Recurrent Neural Networks (RNN)

Long Short-Term Memory (LSTM)

## Regularization: Dropout

In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common



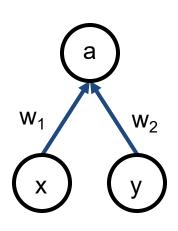


## **Dropout: Test time**

## Compute the expectation

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

 $E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y)$ 



Consider a single neuron.

Without dropout:  $E[a] = w_1x + w_2y$ 

With dropout we have:

At test time, **multiply**by dropout probability  $+ \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y)$   $= \frac{1}{2}(w_1x + w_2y)$ 

## Regularization: A common strategy

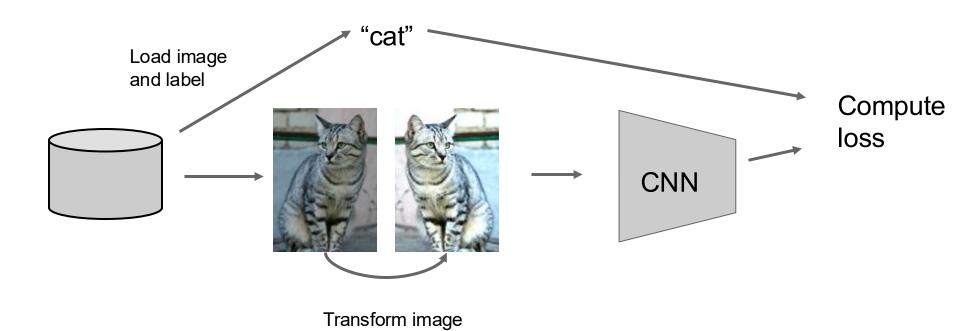
**Training**: Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

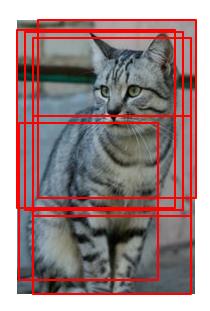
## Regularization: Data Augmentation



# Data Augmentation Random crops and scales

**Training**: sample random crops / scales ResNet:

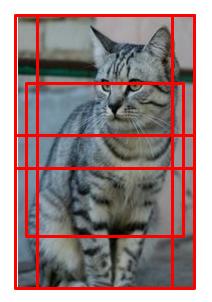
- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



## Data Augmentation Random crops and scales

**Training**: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



#### Testing (test-time augmentation):

take votes / average from a fixed set of crops

- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips
- 3. Make prediction on all crops, use the majority vote as the final output.

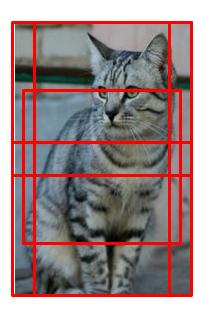
# Data Augmentation Random crops and scales

**Training**: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch

#### Testing (deterministic):

- Take a center crop of 224 by 224.
- Or crop by longer dimension and resize.



#### Gradient clipping: prevent large gradient step

Large gradient step will likely destabilize training (gradients are noisy!)

Large gradient update can be caused by many issues, e.g., large weights, large input, bad loss function / activation function, ...

Should always first try to fix the root cause (normalization, better loss /

activation function, etc.)

But if all things fail ... just clip the gradient

$$g_{new} = \min\left(1, \frac{\lambda}{||g||}\right) \times g$$

g: original gradient

 $\lambda$ : clipping threshold

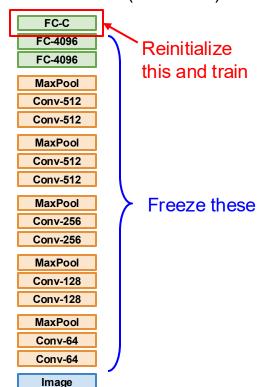
```
# Zero the gradients.
optimizer.zero grad()
# Perform forward pass.
outputs = model(inputs)
# Compute the loss.
loss = loss_function(outputs, targets)
# Perform backward pass (compute gradients).
loss.backward()
# Clip the gradients.
torch.nn.utils.clip_grad_norm_(model.parameters(), max_norm=1.0)
# Update the model parameters.
optimizer.step()
```

#### Transfer Learning with CNNs

1. Train on Imagenet

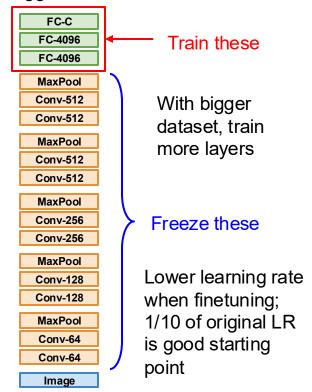
FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64 **Image** 

2. Small Dataset (C classes)



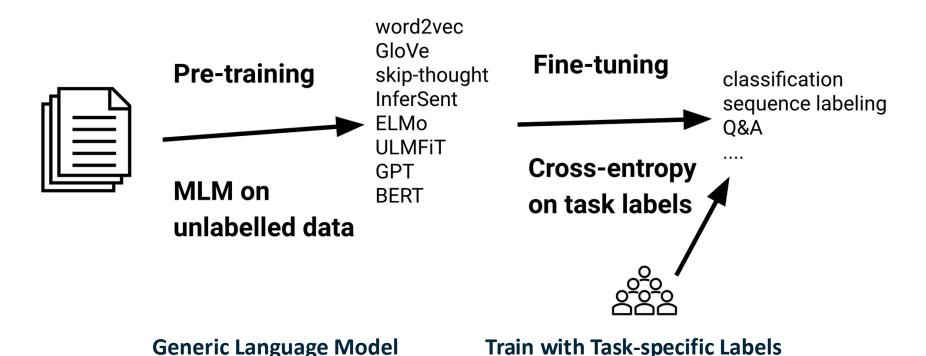
Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

3. Bigger dataset



### Transfer learning is pervasive...

(it's the norm, not an exception)



## Choosing Hyperparameters

Step 1: Check initial loss

Step 2: Overfit a small sample

Step 3: Find LR that makes loss go down

Step 4: Coarse grid, train for ~1-5 epochs

**Step 5**: Refine grid, train longer

Step 6: Look at loss and accuracy curves

Step 7: GOTO step 5

#### Hyperparameters to play with:

- network architecture
- learning rate, its decay schedule, update type
- regularization (L1/L2/Dropout strength)

## Summary

- Improve your training error:
  - Optimizers
  - Learning rate schedules
- Improve your test error:
  - Regularization
  - Choosing Hyperparameters

#### Summary

#### **Training** Deep Neural Networks

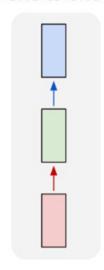
- Details of the non-linear activation functions
- Data normalization
- Weight Initialization
- Batch Normalization
- Advanced Optimization
- Regularization
- Data Augmentation
- Transfer learning
- Hyperparameter Tuning

#### **Next 4 lectures: Sequence Modeling**

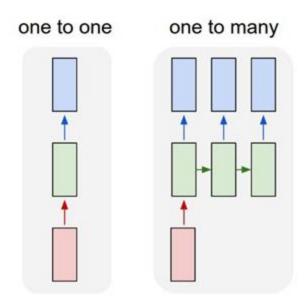
- Recurrent Neural Networks
- Long-short Term Memory
- Transformers
- NLP and Large Language Models

#### "Vanilla" Neural Network

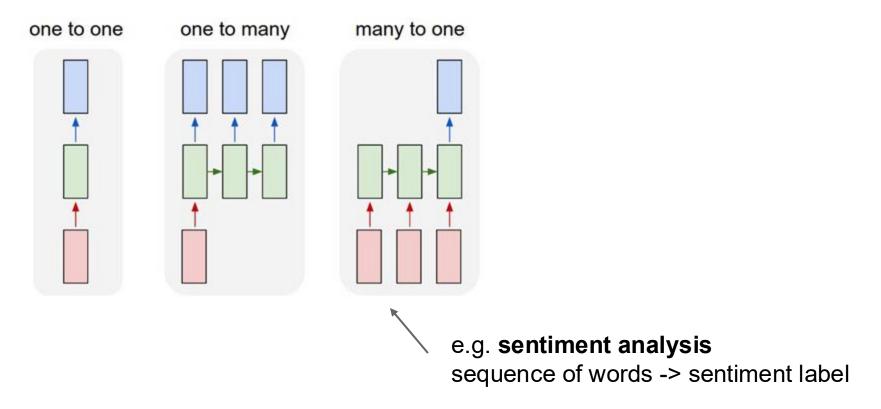
one to one

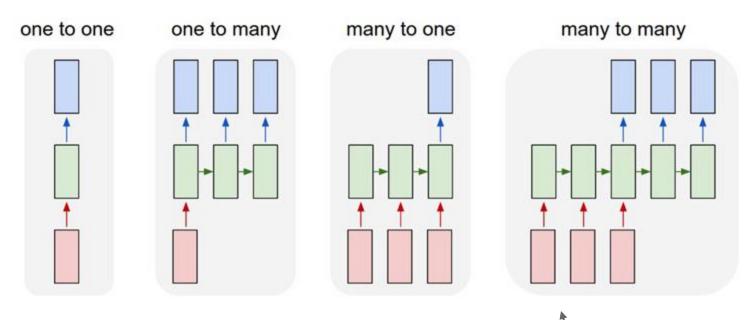


Vanilla Neural Networks

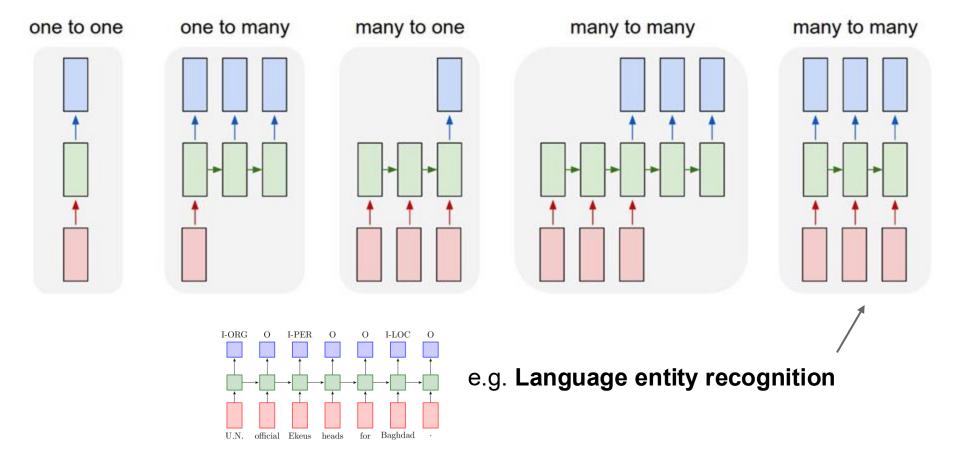


e.g. **Image Captioning** image -> sequence of words





E.g. **Translation, Q&A, Conversation**Sequence of words -> sequence of words



#### Why are existing convnets insufficient?

Variable sequence length inputs and outputs!

**Example task**: video captioning

**Input** video can have variable number of frames

Output captions can be variable length.

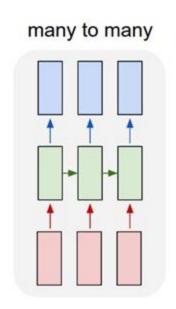


Output Captions

A lady joins the man and sings along to the music.

#### Let's start with a setting that takes a variable input and produces an output at every step

Example: Video activity labeling





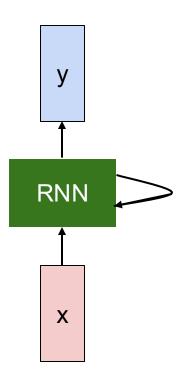
Huang et al., 2016

**Input**: video frame; **Output**: activity label at each frame Recognizing an activity requires looking at more than one frame!

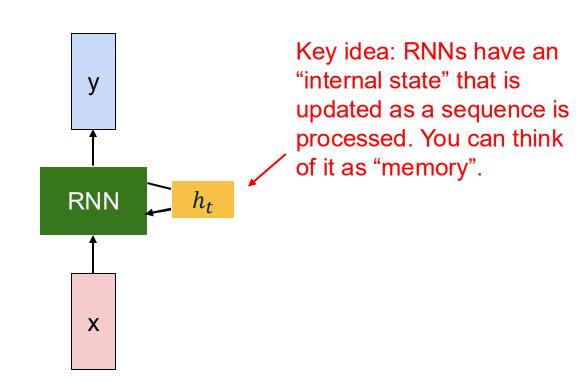
Want: a model that can make prediction for each frame based on the past frames.

We need a model that can memorize what it has seen so far!

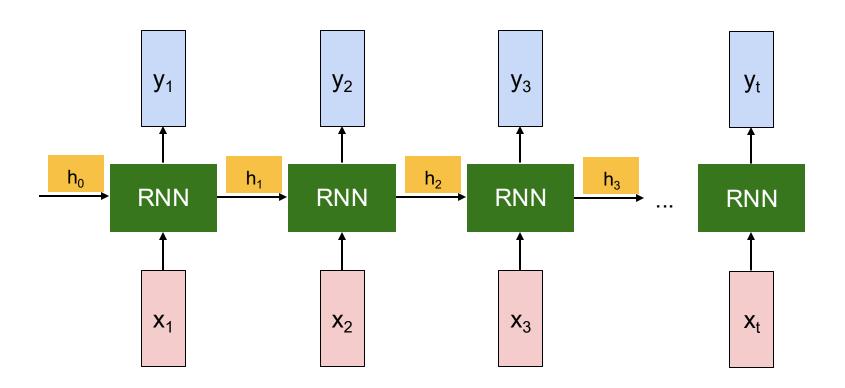
#### Recurrent Neural Network



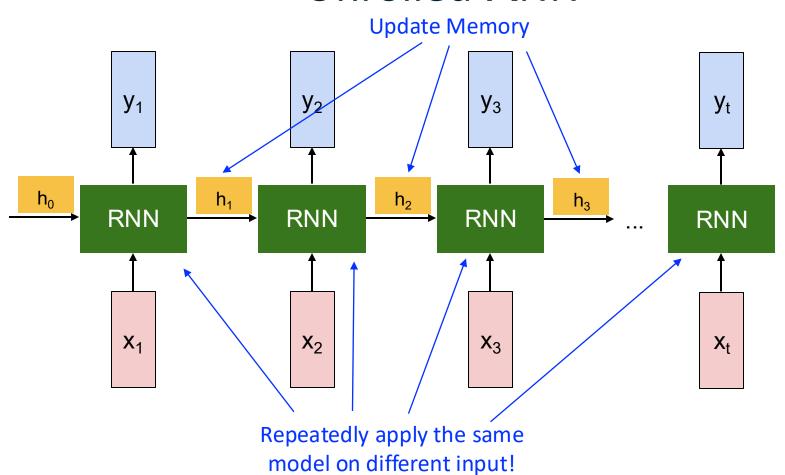
#### Recurrent Neural Network



#### **Unrolled RNN**



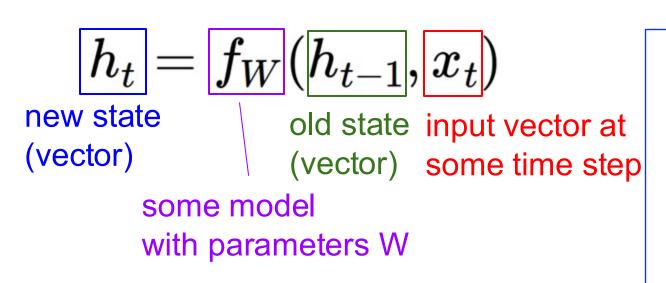
#### **Unrolled RNN**



### RNN hidden state update

**RNN** 

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:



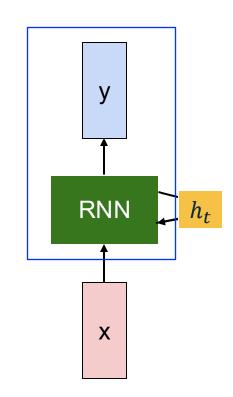
Can set initial state  $h_0$  to all 0's

### RNN output generation

"Read out" the prediction by passing the hidden state through a network (e.g., a few FC layers)

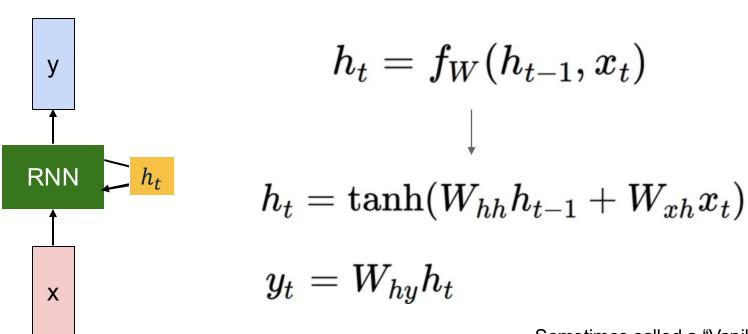
$$y_{t} = f_{W_{hy}}(h_{t})$$
output
new state
another model
with parameters  $W_{hy}$ 

The prediction network is often shared across timestep.

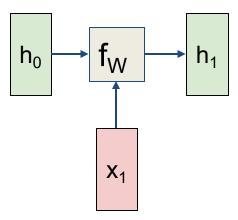


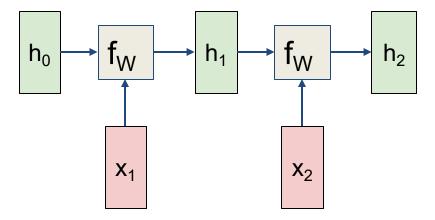
## (Simple) Recurrent Neural Network

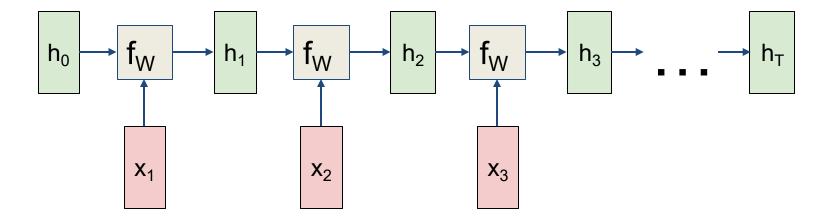
The state consists of a single "hidden" vector **h**:



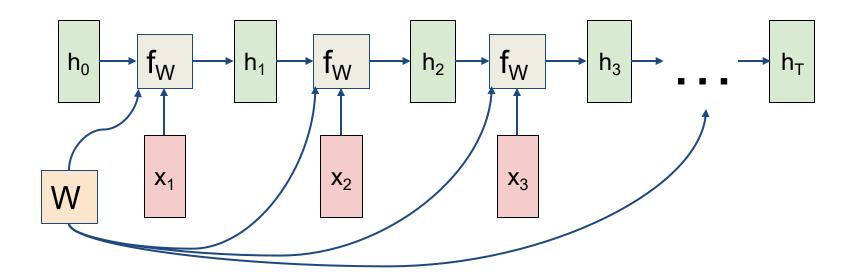
Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman



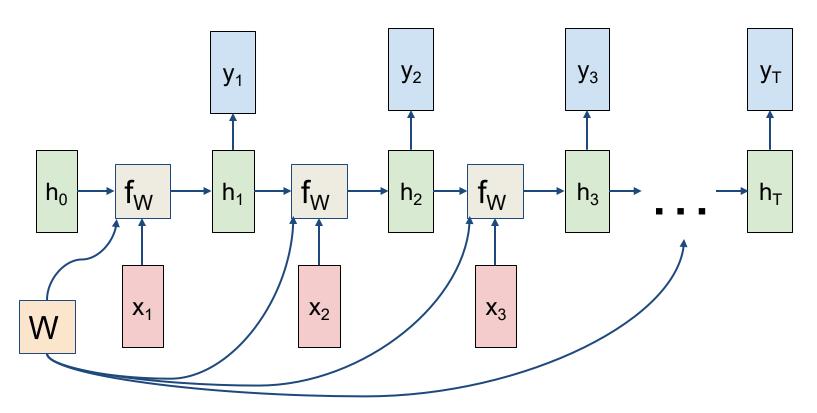




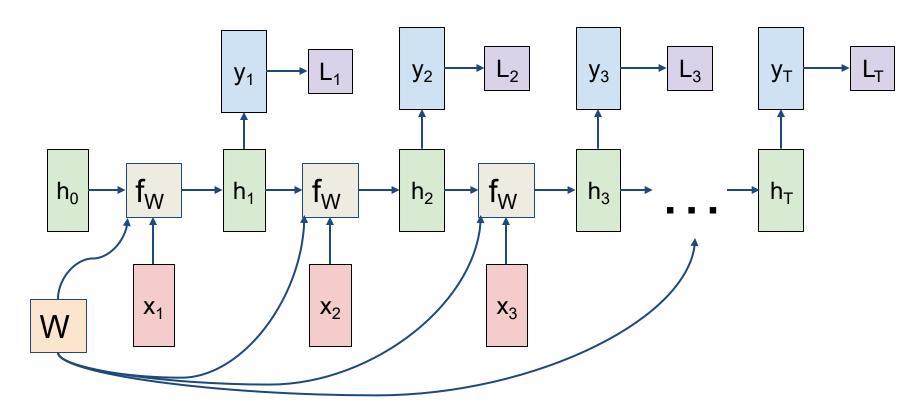
Re-use the same weight matrix at every time-step



#### RNN: Computational Graph: Many to Many

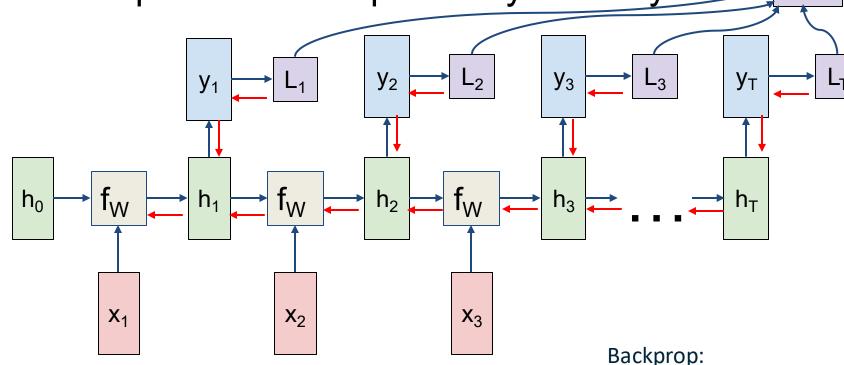


#### RNN: Computational Graph: Many to Many



#### RNN: Computational Graph: Many to Many **y**<sub>2</sub> **y**<sub>3</sub> $f_W$ $f_W$ $h_3$ $h_2$ $h_0$ $h_1$ $T_W$ $X_2$ $X_1$ $X_3$ W Backprop:

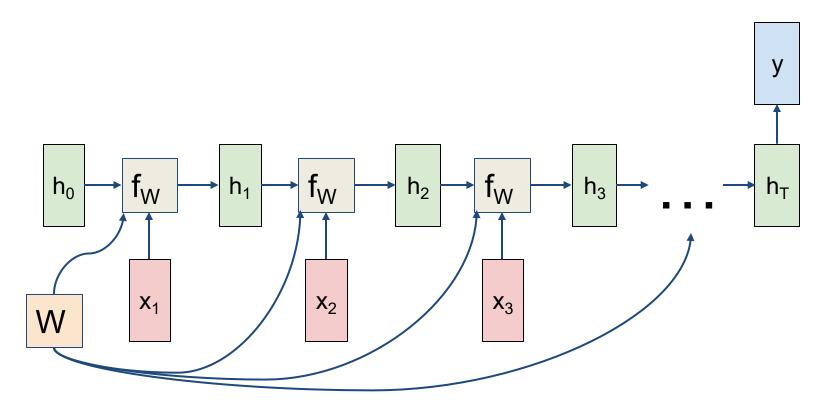
RNN: Computational Graph: Many to Many



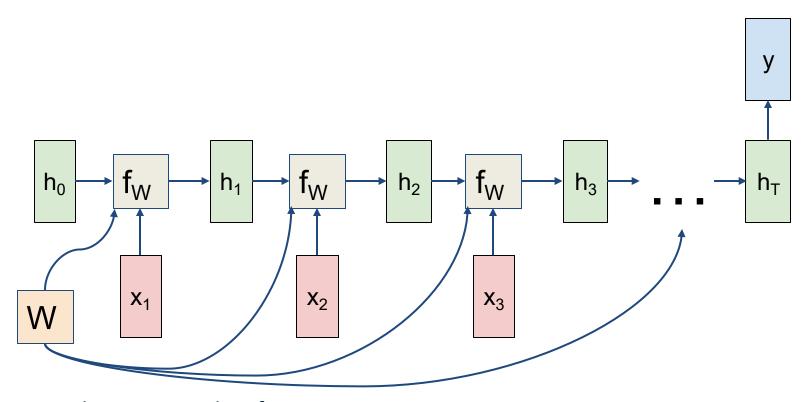
 $f_W$  receives gradients from both current-step prediction loss and loss from future steps!

$$\frac{\partial L}{\partial W_i} = \sum\nolimits_{t=i}^T \frac{\partial L_t}{\partial W_i}$$

#### RNN: Computational Graph: Many to One

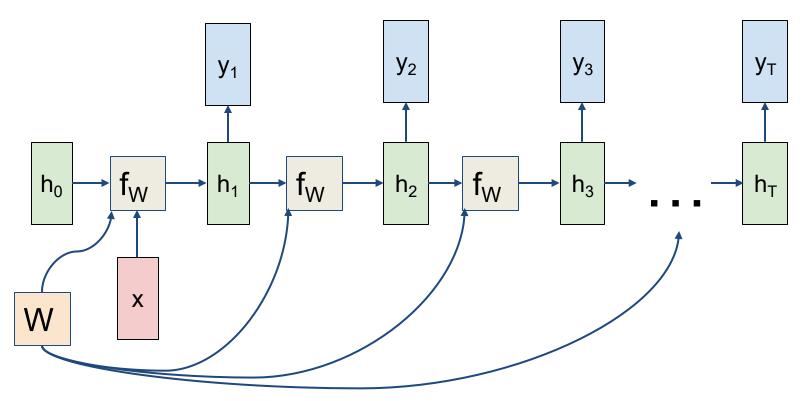


# RNN: Computational Graph: Many to One



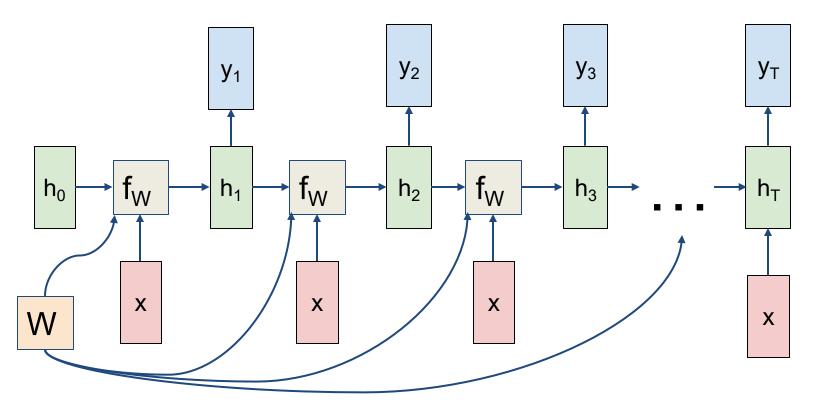
Example: sentence classification

# RNN: Computational Graph: One to Many



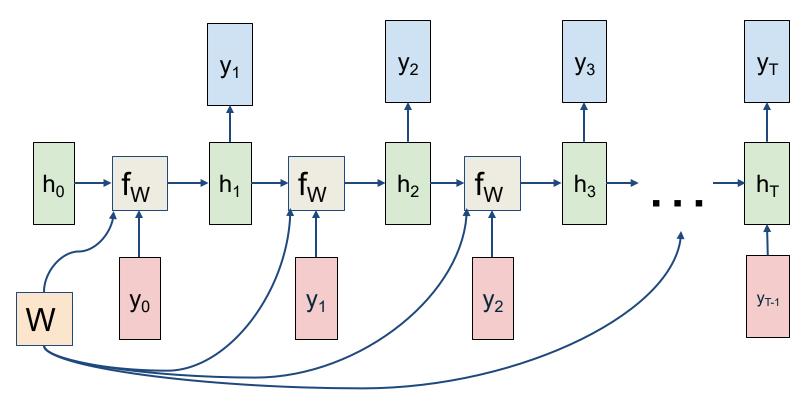
Example: image captioning

# RNN: Computational Graph: One to Many



Example: image captioning

# RNN: Computational Graph: One to Many

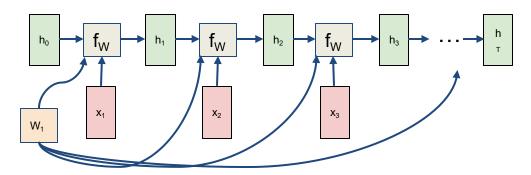


Example: text generation

# Sequence to Sequence: Many-to-one + one-tomany

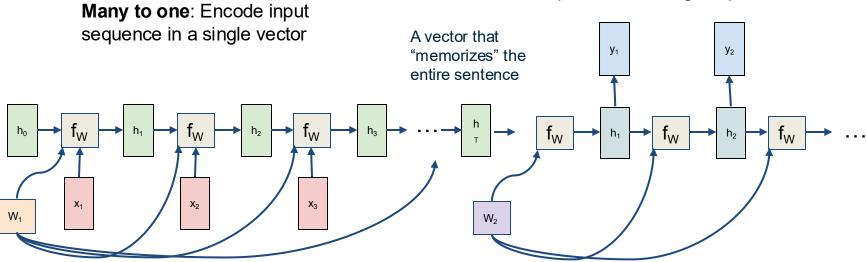
**Many to one**: Encode input sequence in a single vector

A vector that "memorizes" the entire sentence



# Sequence to Sequence: Many-to-one + one-tomany

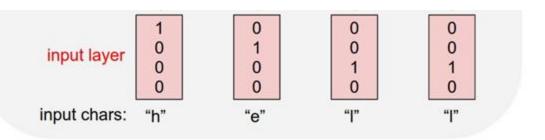
One to many: Produce output sequence from single input vector



#### Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: "hello" with one-hot encoding

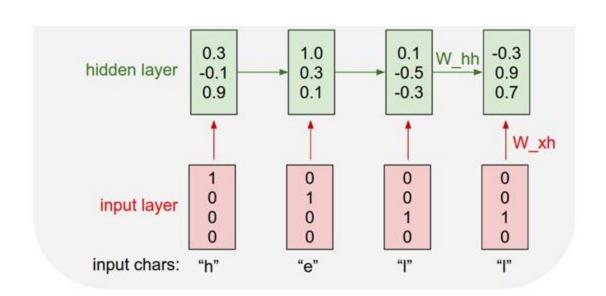


#### Example: Character-level Language Model

$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

Vocabulary: [h,e,l,o]

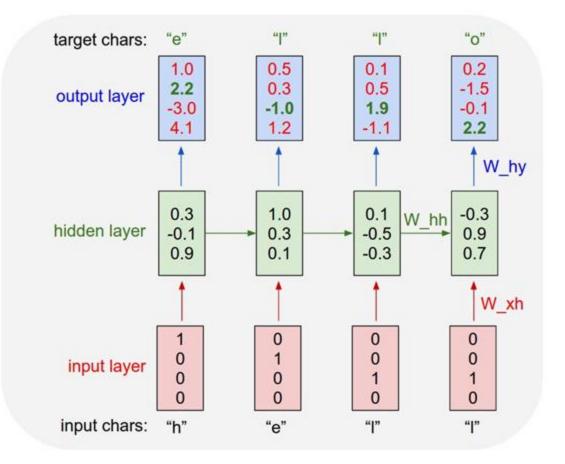
Example training sequence: "hello" with one-hot encoding



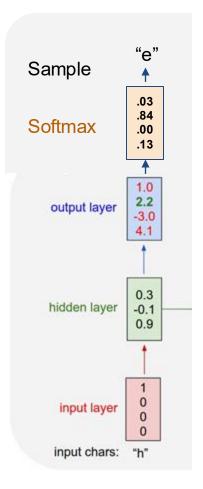
#### Example: Character-level Language Model

Vocabulary: [h,e,l,o]

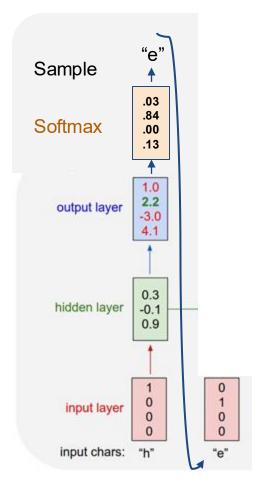
Example training sequence: "hello" with one-hot encoding



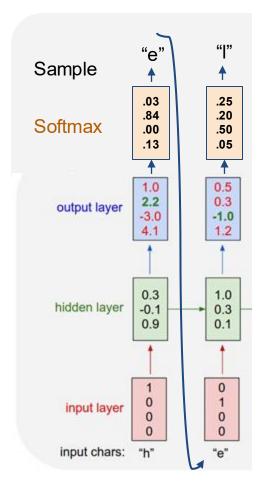
Vocabulary: [h,e,l,o]



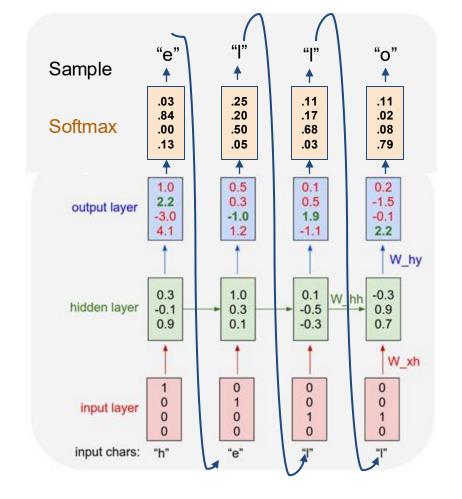
Vocabulary: [h,e,l,o]

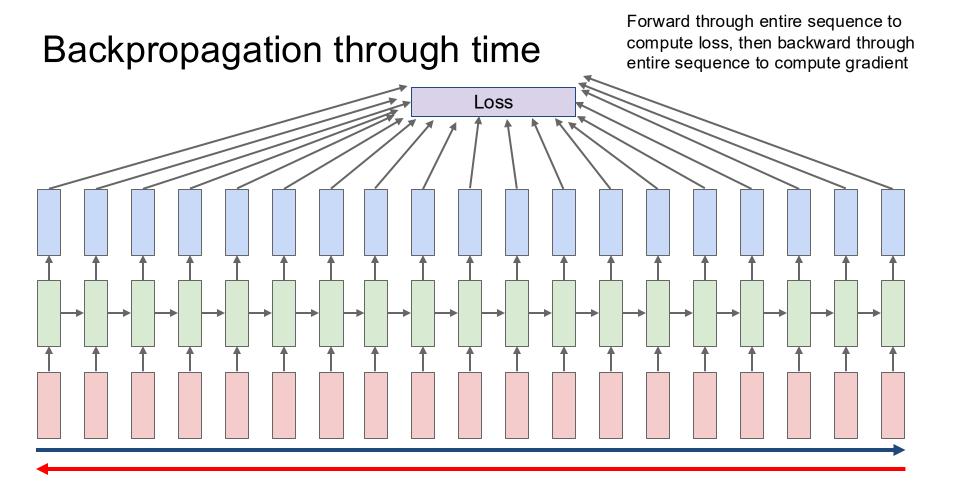


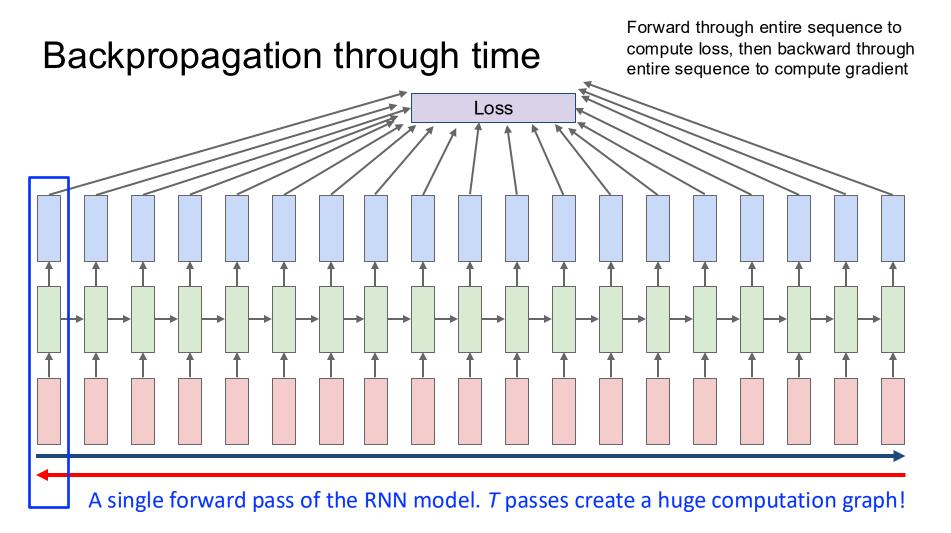
Vocabulary: [h,e,l,o]

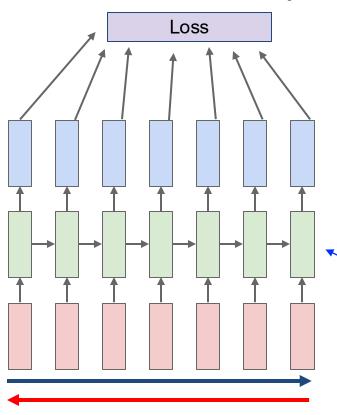


Vocabulary: [h,e,l,o]



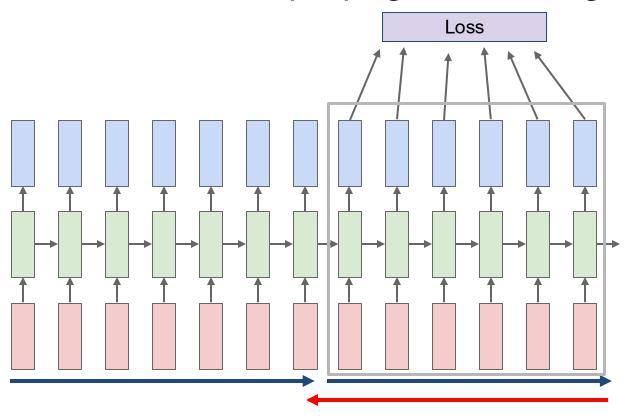




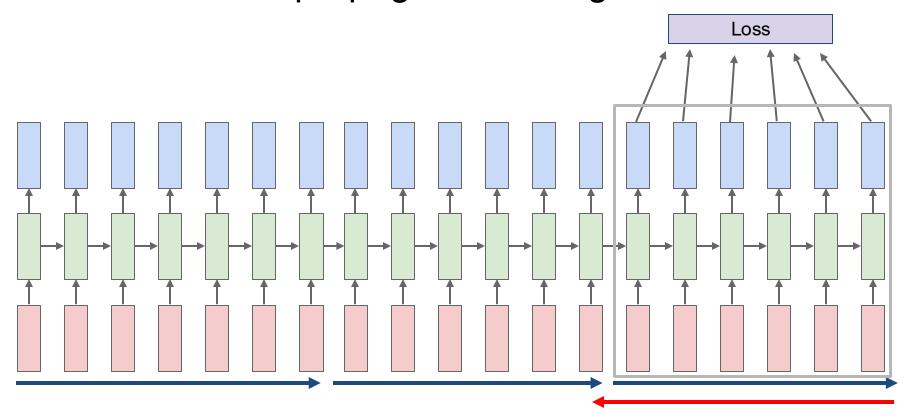


Run forward and backward through chunks (length k) of the sequence instead of whole sequence, do parameter update, clear gradient cache

Save the last hidden state!

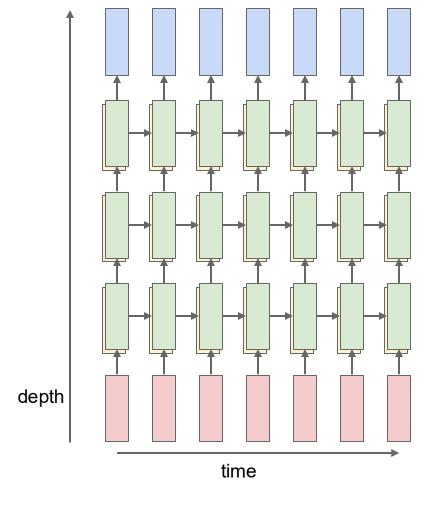


Carry hidden states forward in time for k steps, backprop, update parameter, clear gradient ...



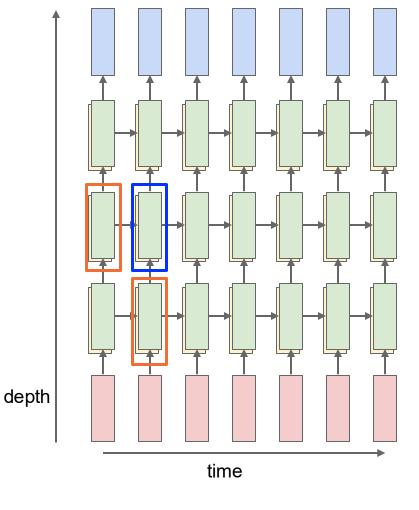
```
# pseudocode for Truncated BPTT
2 | h = h 0
   for c_i in num_chunk:
       start_i, end_i = c_i * chunk_size, (c_i + 1) * chunk_size
       for i in range(start_i, end_i):
5
6
7
           h = f_h(x[i], h)
           y pred[i] = f y(h)
8
       L = compute_loss(y_pred[start_i:end_i], y[start_i:end_i])
       backprop_update(L, [f_h, f_y])
       clear_gradient([f_h, f_y])
10
```

## Multilayer RNNs



#### Multilayer RNNs

Each RNN layer takes as input (1) previous hidden state from the same layer and (2) the output of the previous layer at the same timestep (or the input).



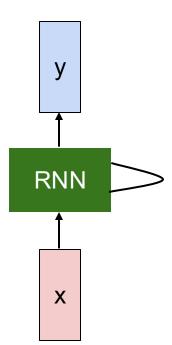
#### THE SONNETS

#### by William Shakespeare

From fairest creatures we desire increase,
That thereby beauty's rose might never die,
But as the riper should by time decease,
His tender heir might bear his memory:
But thou, contracted to thine own bright eyes,
Feed'st thy light's flame with self-substantial fuel,
Making a famine where abundance lies,
Thyself thy foe, to thy sweet self too cruel:
Thou that art now the world's fresh ornament,
And only herald to the gaudy spring,
Within thine own bud buriest thy content,
And tender churl mak'st waste in niggarding:
Pity the world, or else this glutton be,
To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery so gazed on now, Will be a tatter'd weed of small worth held: Then being asked, where all thy beauty lies, Where all the treasure of thy lusty days; To say, within thine own deep sunken eyes, Were an all-eating shame, and thriftless praise. How much more praise deserv'd thy beauty's use, If thou couldst answer 'This fair child of mine Shall sum my count, and make my old excuse,' Proving his beauty by succession thine!

This were to be new made when thou art old, And see thy blood warm when thou feel'st it cold.



at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

#### train more

"Tmont thithey" fomesscerliund
Keushey. Thom here
sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome
coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

#### train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

#### train more

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him.

Pierre aking his soul came to the packs and drove up his father-in-law women.

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

DUKE VINCENTIO: Well, your wit is in the care of side and that.

Second Lord:

They would be ruled after this chamber, and my fair nues begun out of the fact, to be conveyed, Whose noble souls I'll have the heart of the wars.

Come, sir, I will make did behold your worship.

I'll drink it.

Clown:

VIOLA:

PANDARUS:

Second Senator:

VIOLA:

KING LEAR:

Why, Salisbury must find his flesh and thought That which I am not aps, not a man and in fire, To show the reining of the raven and the wars

We spare with hours, but cut thy council I am great,

To grace my hand reproach within, and not a fair are hand, That Caesar and my goodly father's world;

When I was heaven of presence and our fleets,

Murdered and by thy master's ready there My power to give thee but so much as hell:

Some service in the noble bondman here,

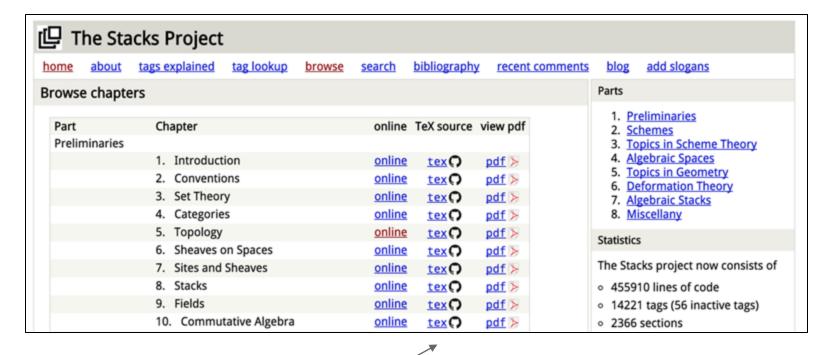
Would show him to her wine.

Shall be against your honour.

O, if you were a feeble sight, the courtesy of your law, Your sight and several breath, will wear the gods With his heads, and my hands are wonder'd at the deeds,

So drop upon your lordship's head, and your opinion

#### The Stacks Project: open source algebraic geometry textbook



Latex source

http://stacks.math.columbia.edu/

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For  $\bigoplus_{n=1,...,m}$  where  $\mathcal{L}_{m_{\bullet}} = 0$ , hence we can find a closed subset  $\mathcal{H}$  in  $\mathcal{H}$  and any sets  $\mathcal{F}$  on X, U is a closed immersion of S, then  $U \to T$  is a separated algebraic space.

Proof. Proof of (1). It also start we get

$$S = \operatorname{Spec}(R) = U \times_X U \times_X U$$

and the comparison in the fibre product covering we have to prove the lemma generated by  $\coprod Z \times_U U \to V$ . Consider the maps M along the set of points  $Sch_{fppf}$  and  $U \to U$  is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset  $W \subset U$  in Sh(G) such that  $Spec(R') \to S$  is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that  $f_i$  is of finite presentation over S. We claim that  $\mathcal{O}_{X,x}$  is a scheme where  $x,x',s''\in S'$  such that  $\mathcal{O}_{X,x'}\to \mathcal{O}'_{X',x'}$  is separated. By Algebra, Lemma ?? we can define a map of complexes  $\mathrm{GL}_{S'}(x'/S'')$ 

To prove study we see that  $\mathcal{F}|_U$  is a covering of  $\mathcal{X}'$ , and  $\mathcal{T}_i$  is an object of  $\mathcal{F}_{X/S}$  for i > 0 and  $\mathcal{F}_p$  exists and let  $\mathcal{F}_i$  be a presheaf of  $\mathcal{O}_X$ -modules on  $\mathcal{C}$  as a  $\mathcal{F}$ -module. In particular  $\mathcal{F} = U/\mathcal{F}$  we have to show that

$$\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\operatorname{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$$

is a unique morphism of algebraic stacks. Note that

$$Arrows = (Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$$

and

and we win.

$$V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by  $X_{spaces, \ell tale}$  which gives an open subspace of X and T equal to  $S_{Zar}$ , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S. Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose  $X = \lim |X|$  (by the formal open covering X and a single map  $\underline{Proj}_X(A) = \operatorname{Spec}(B)$  over U compatible with the complex

$$Set(A) = \Gamma(X, \mathcal{O}_{X,\mathcal{O}_X}).$$

When in this case of to show that  $Q \to C_{Z/X}$  is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S. Moreover there exists a closed subspace  $Z \subset X$  of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

*Proof.* This is form all sheaves of sheaves on X. But given a scheme U and a surjective étale morphism  $U \to X$ . Let  $U \cap U = \coprod_{i=1,...,n} U_i$  be the scheme X over S at the schemes  $X_i \to X$  and  $U = \lim_i X_i$ .

The following lemma surjective restrocomposes of this implies that  $F_{x_0} = F_{x_0} = F_{x_0}$ .

**Lemma 0.2.** Let X be a locally Noetherian scheme over S,  $E = \mathcal{F}_{X/S}$ . Set  $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$ . Since  $\mathcal{I}^n \subset \mathcal{I}^n$  are nonzero over  $i_0 \leq \mathfrak{p}$  is a subset of  $\mathcal{J}_{n,0} \circ \overline{A}_2$  works.

Lemma 0.3. In Situation ??. Hence we may assume q' = 0.

Proof. We will use the property we see that p is the mext functor (??). On the other hand, by Lemma ?? we see that

$$D(O_{X'}) = O_X(D)$$

where K is an F-algebra where  $\delta_{n+1}$  is a scheme over S.

Lemma 0.1. Let C be a set of the construction.

Let C be a gerber covering. Let F be a quasi-coherent sheaves of O-modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

Proof. This is an algebraic space with the composition of sheaves F on  $X_{\acute{e}tale}$  we have

$$O_X(\mathcal{F}) = \{morph_1 \times_{O_X} (\mathcal{G}, \mathcal{F})\}$$

where G defines an isomorphism  $F \to F$  of O-modules.

Lemma 0.2. This is an integer Z is injective.

**Lemma 0.3.** Let S be a scheme. Let X be a scheme and X is an affine open covering. Let  $U \subset X$  be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

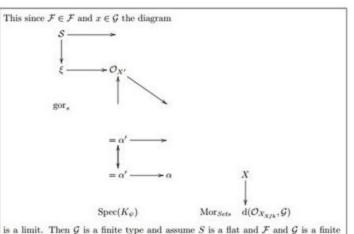
$$b: X \to Y' \to Y \to Y \to Y' \times_X Y \to X.$$

be a morphism of algebraic spaces over S and Y.

Proof. Let X be a nonzero scheme of X. Let X be an algebraic space. Let F be a quasi-coherent sheaf of  $O_X$ -modules. The following are equivalent

- F is an algebraic space over S.
- (2) If X is an affine open covering.

Consider a common structure on X and X the functor  $\mathcal{O}_X(U)$  which is locally of finite type.



type f.. This is of finite type diagrams, and

- the composition of G is a regular sequence,
- O<sub>X'</sub> is a sheaf of rings.

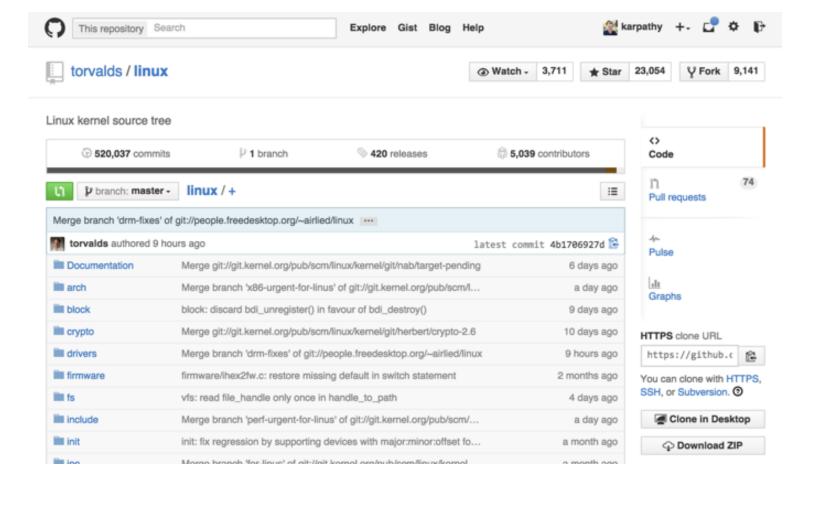
Proof. We have see that  $X = \operatorname{Spec}(R)$  and  $\mathcal{F}$  is a finite type representable by algebraic space. The property  $\mathcal{F}$  is a finite morphism of algebraic stacks. Then the cohomology of X is an open neighbourhood of U.

Proof. This is clear that G is a finite presentation, see Lemmas ??. A reduced above we conclude that U is an open covering of C. The functor F is a "field"

$$\mathcal{O}_{X,x} \longrightarrow \mathcal{F}_{\mathbb{Z}} \quad \text{-1}(\mathcal{O}_{X_{deale}}) \longrightarrow \mathcal{O}_{X_{d}}^{-1}\mathcal{O}_{X_{\lambda}}(\mathcal{O}_{X_{u}}^{\mathbb{Z}})$$
  
is an isomorphism of covering of  $\mathcal{O}_{X_{d}}$ . If  $\mathcal{F}$  is the unique element of  $\mathcal{F}$  such that  $X$ 

is an isomorphism. The property  $\mathcal{F}$  is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme  $\mathcal{O}_X$ -algebra with  $\mathcal{F}$  are opens of finite type over S.  $\Pi$   $\mathcal{F}$  is a scheme theoretic image points.

If  $\mathcal{F}$  is a finite direct sum  $\mathcal{O}_{X_{\lambda}}$  is a closed immersion, see Lemma ??. This is a sequence of  $\mathcal{F}$  is a similar morphism.



```
static void do command(struct seq file *m, void *v)
 int column = 32 << (cmd[2] & 0x80);
 if (state)
    cmd = (int)(int state ^ (in 8(&ch->ch flags) & Cmd) ? 2 : 1);
 else
    seq = 1;
 for (i = 0; i < 16; i++) {
   if (k & (1 << 1))
      pipe = (in use & UMXTHREAD UNCCA) +
        ((count & 0x0000000ffffffff8) & 0x000000f) << 8;
    if (count == 0)
      sub(pid, ppc md.kexec handle, 0x20000000);
    pipe set bytes(i, 0);
  /* Free our user pages pointer to place camera if all dash */
  subsystem info = &of changes[PAGE SIZE];
  rek controls(offset, idx, &soffset);
  /* Now we want to deliberately put it to device */
 control check polarity(&context, val, 0);
  for (i = 0; i < COUNTER; i++)
    seq puts(s, "policy ");
```

# Generated C code

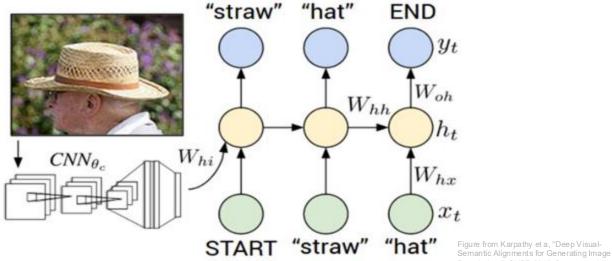
```
Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
    This program is free software; you can redistribute it and/or modify it
* under the terms of the GNU General Public License version 2 as published by
* the Free Software Foundation.
         This program is distributed in the hope that it will be useful,
 * but WITHOUT ANY WARRANTY; without even the implied warranty of
    MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
   GNU General Public License for more details.
    You should have received a copy of the GNU General Public License
     along with this program; if not, write to the Free Software Foundation,
* Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
*/
#include linux/kexec.h>
#include inux/errno.h>
#include ux/io.h>
#include inux/platform device.h>
#include inux/multi.h>
#include linux/ckevent.h>
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
```

10

```
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
#define REG PG vesa slot addr pack
#define PFM NOCOMP AFSR(0, load)
#define STACK DDR(type) (func)
#define SWAP_ALLOCATE(nr)
                           (e)
#define emulate sigs() arch get unaligned child()
#define access rw(TST) asm volatile("movd %%esp, %0, %3" : : "r" (0)); \
 if (_type & DO_READ)
static void stat PC SEC    read mostly offsetof(struct seq argsqueue, \
         pC>[1]);
static void
os_prefix(unsigned long sys)
#ifdef CONFIG PREEMPT
 PUT_PARAM_RAID(2, sel) = get_state_state();
 set_pid_sum((unsigned long)state, current_state_str(),
          (unsigned long)-1->lr_full; low;
```

#include <asm/io.h>
#include <asm/prom.h>

# Image Captioning



Descriptions", CVPR 2015; figure copyrightee, 2015.

Reproduced for educational purposes.

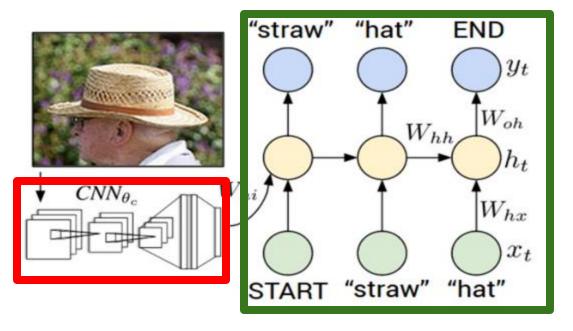
Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei
Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

#### **Recurrent Neural Network**



**Convolutional Neural Network** 



test image

This image is CC0 public domain

image conv-64 conv-64 maxpool conv-128 conv-128 maxpool conv-256 conv-256 maxpool conv-512 conv-512 maxpool conv-512 conv-512 maxpool FC-4096 FC-4096 FC-1000

softmax



test image

image conv-64 conv-64 maxpool conv-128 conv-128 maxpool conv-256 conv-256 maxpool conv-512 conv-512 maxpool conv-512 conv-512 maxpool FC-4096 FC-4096 FC-1000



test image

image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

maxpool

conv-512

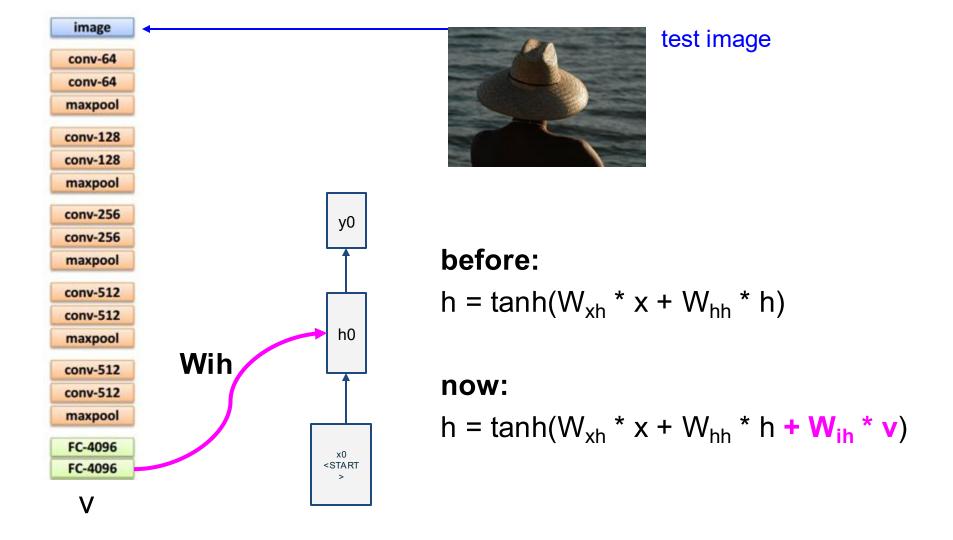
maxpool

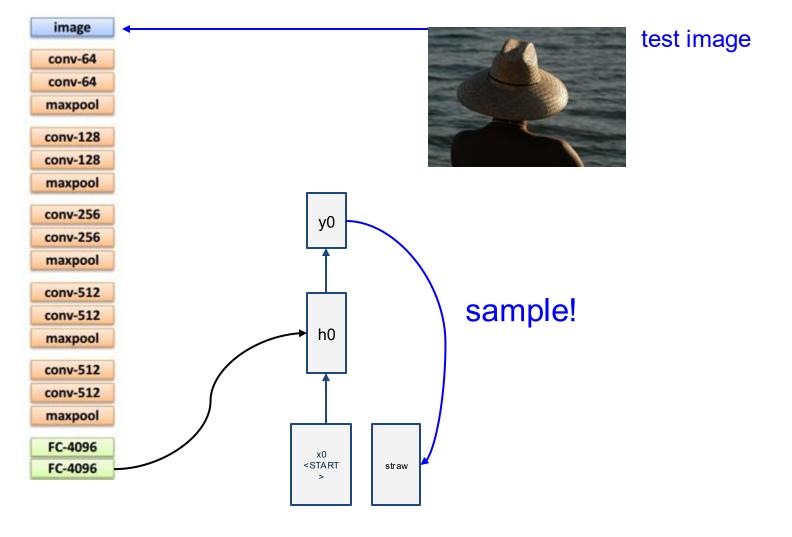
FC-4096 FC-4096

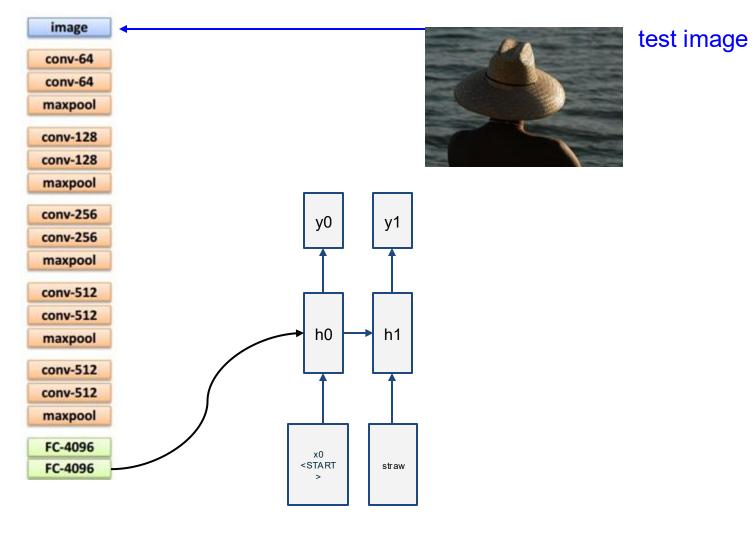


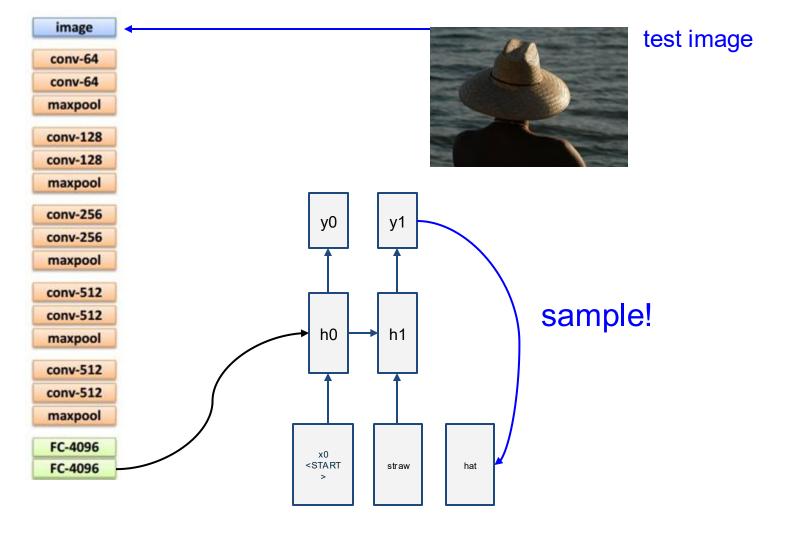
test image

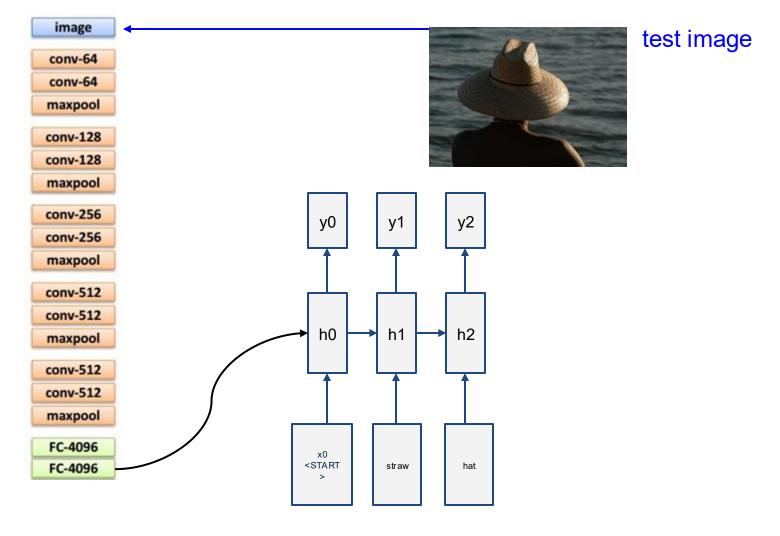
x0 <START >

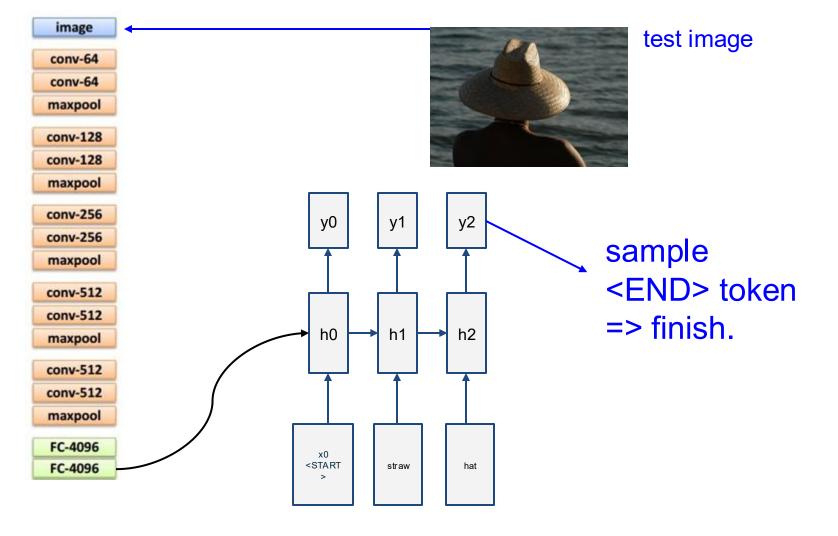












## Image Captioning: Example Results





A cat sitting on a suitcase on the floor



A cat is sitting on a tree branch



A dog is running in the grass with a frisbee



A white teddy bear sitting in the grass



Two people walking on the beach with surfboards



A tennis player in action on the court



Two giraffes standing in a grassy field



A man riding a dirt bike on a dirt track

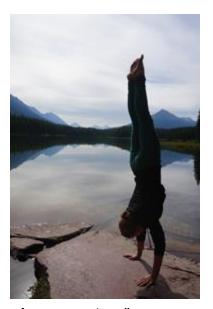
# Image Captioning: Failure Cases



A woman is holding a cat in her hand



A person holding a computer mouse on a desk



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch



A man in a baseball uniform throwing a ball

## Visual Question Answering (VQA)



Q: What endangered animal is featured on the truck?

- A: A bald eagle.
- A: A sparrow.
- A: A humming bird.
- A: A raven.



Q: Where will the driver go if turning right?

- A: Onto 24 3/4 Rd.
- A: Onto 25 3/4 Rd.
- A: Onto 23 3/4 Rd.
- A: Onto Main Street.



Q: When was the picture taken?

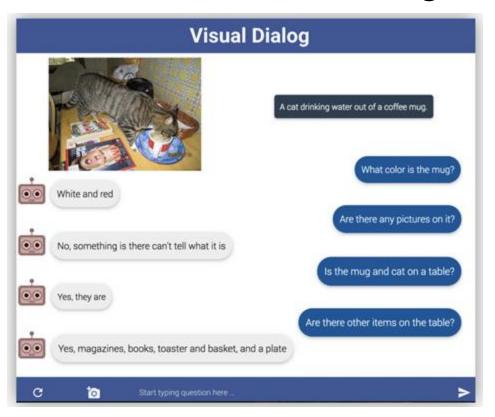
- A: During a wedding.
- A: During a bar mitzvah.
- A: During a funeral.
- A: During a Sunday church



Q: Who is under the umbrella?

- A: Two women.
- A: A child.
- A: An old man.
- A: A husband and a wife.

### Visual Dialog: Conversations about images



Das et al, "Visual Dialog", CVPR 2017
Figures from Das et al, copyright IEEE 2017. Reproduced with permission.

## Visual Language Navigation: Go to the living room

Agent encodes instructions in language and uses an RNN to generate a series of movements as the visual input changes after each move.

#### Instruction

Turn right and head towards the kitchen. Then turn left, pass a table and enter the hallway. Walk down the hallway and turn into the entry way to your right without doors. Stop in front of the toilet.

> Initial Position **Target Position**

Local visual scene



Wang et al, "Reinforced Cross-Modal Matching and Self-Supervised Imitation Learning for Vision-Language Navigation", CVPR 2018 Figures from Wang et al, copyright IEEE 2017. Reproduced with permission.

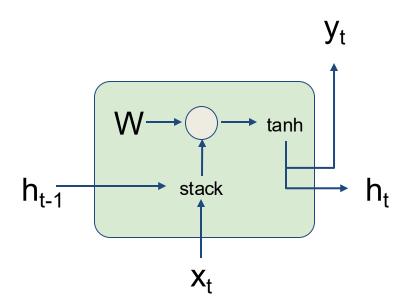
#### RNN tradeoffs

#### **RNN** Advantages:

- Can process any length input
- Computation for step t can (in theory) use information from many steps back
- Model size doesn't increase for longer input
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

#### RNN Disadvantages:

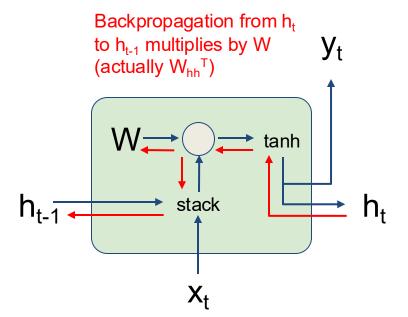
- Recurrent computation is slow
- In practice, difficult to access information from many steps back
- Vanishing gradient / gradient explosion



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

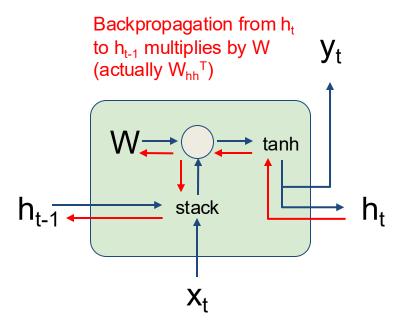
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$= \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

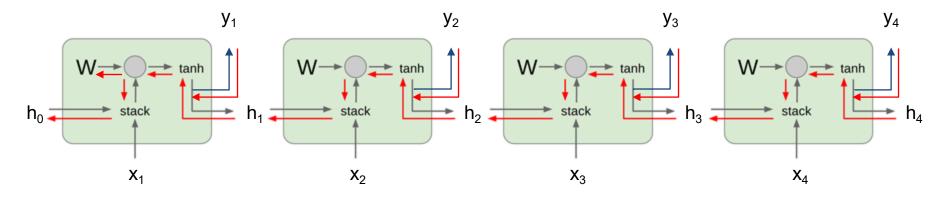


$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

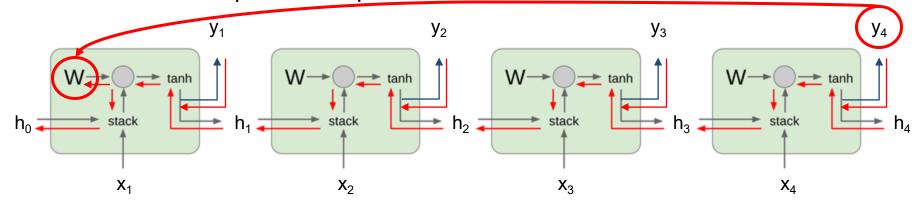
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1} + W_{xh}x_t)W_{hh}$$



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

Gradients over multiple time steps:

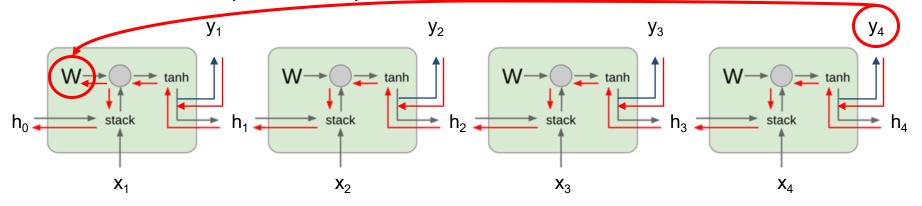


$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W}$$

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:

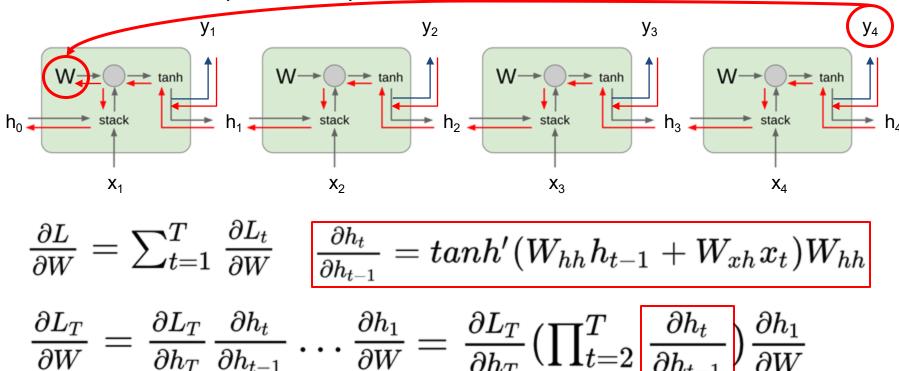


$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W} = rac{\partial L_T}{\partial h_T} (\prod_{t=2}^T rac{\partial h_t}{\partial h_{t-1}}) rac{\partial h_1}{\partial W}$$

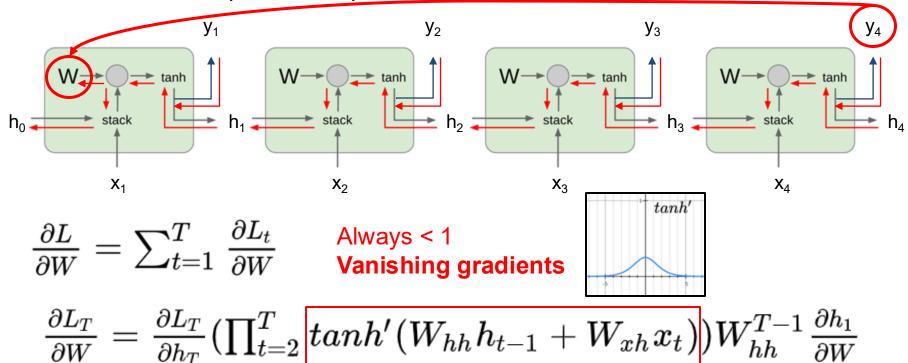
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



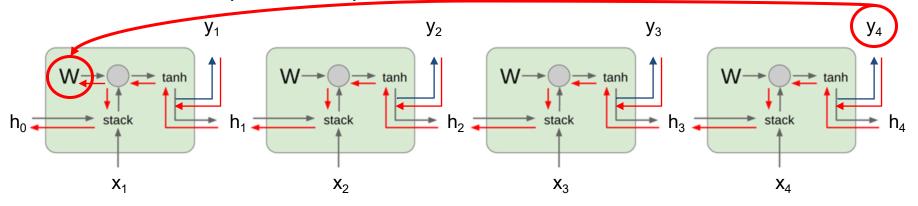
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:

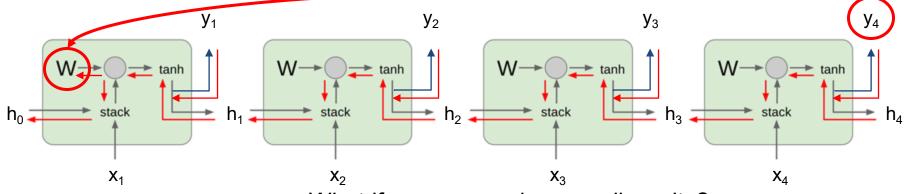


$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

What if we assumed no non-linearity?

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



What if we assumed no non-linearity?

$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

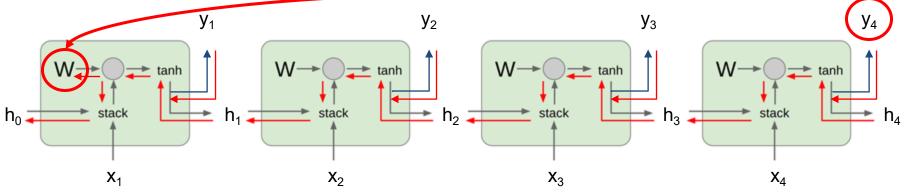
Largest eigen value > 1: **Exploding gradients** 

 $rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$ 

Largest eigen value < 1: Vanishing gradients

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



What if we assumed no non-linearity?

$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest eigen value > 1: **Exploding gradients** 

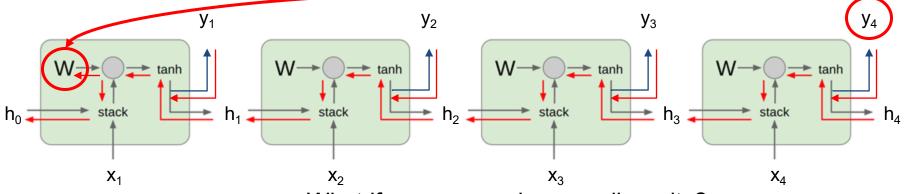
Largest eigen value < 1: Vanishing gradients

→ Gradient clipping: Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)
if grad_norm > threshold:
    grad *= (threshold / grad_norm)
```

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest eigen value > 1: **Exploding gradients** 

→ We need a new RNN architecture!

### Long-Short Term Memory (Incomplete)

RNN directly updates  $h_t$  through **multiplying** with a weight matrix:

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1} + W_{xh}x_t)W_{hh}$$

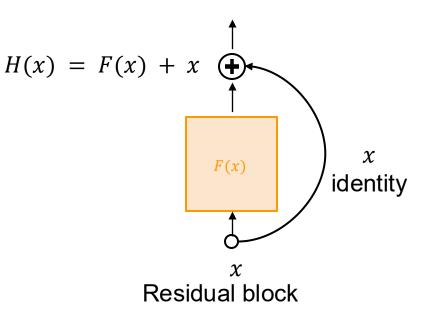
LSTM keeps track of a cell state  $c_t$  that's updated through addition

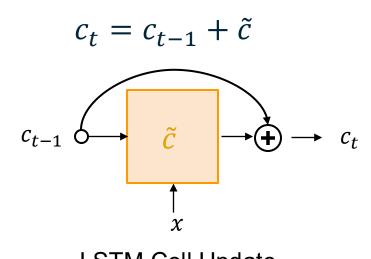
$$c_t = c_{t-1} + \tilde{c}$$
  

$$\tilde{c} = \tanh(W[h_{t-1}, x_t]), h_t = \tanh(c_t)$$

Gradient of cell state: 
$$\frac{\partial c_t}{\partial c_{t-1}} = 1 + \frac{\partial \tilde{c}}{\partial c_{t-1}}$$
 This should look familiar ... Residual connection!

## Long-Short Term Memory (Incomplete)





LSTM Cell Update

 $\tilde{c} = \tanh(W[h_{t-1}, x_t]), h_t = \tanh(c_t)$ 

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

#### **LSTM**

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

Have "gates" to control information flow from previous state to the next state

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

LSTM

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

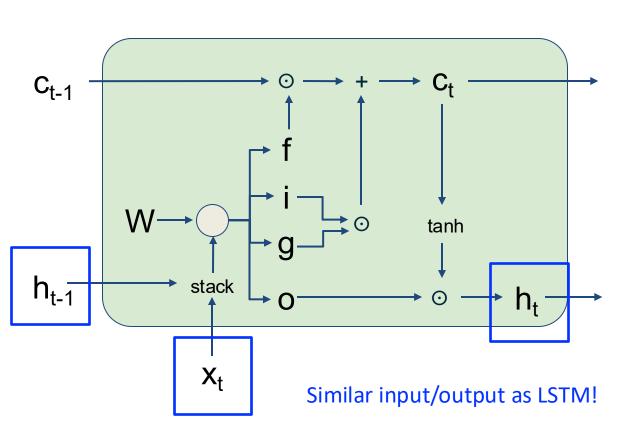
$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

Long-term memory *c* determines how much information should go into the hidden state *h* (short-term memory)

Two "memory vectors"

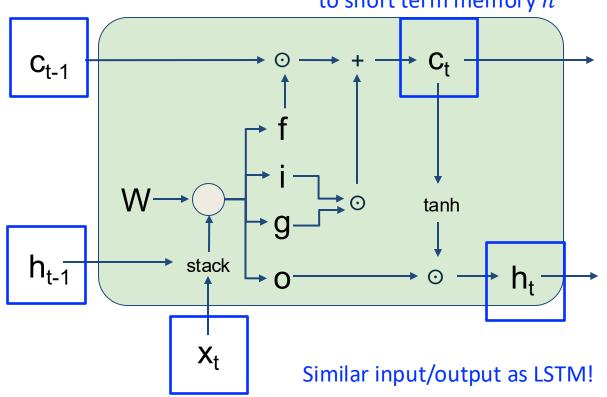
[Hochreiter et al., 1997]



$$c_t = f_t \odot c_{t-1} + i_t \odot g_t$$
$$h_t = o_t \odot \tanh(c_t)$$

[Hochreiter et al., 1997]

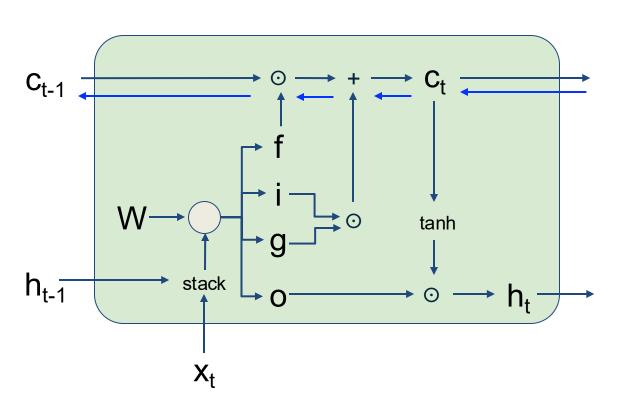
Keep long-term memory cell c in addition to short term memory h



$$c_t = f_t \odot c_{t-1} + i_t \odot g_t$$
$$h_t = o_t \odot \tanh(c_t)$$

#### Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]



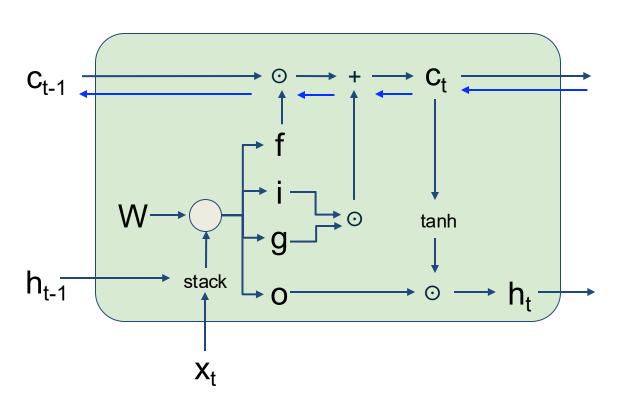
Backpropagation from  $c_t$  to  $c_{t-1}$  only elementwise multiplication by f (forget gate), no matrix multiply by W

$$c_t = f_t \odot c_{t-1} + i_t \odot g_t$$
$$h_t = o_t \odot \tanh(c_t)$$

$$\frac{\partial c_t}{\partial c_{t-1}} = \frac{1}{2}$$

### Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]



Backpropagation from  $c_t$  to  $c_{t-1}$  only elementwise multiplication by f (forget gate), no matrix multiply by W

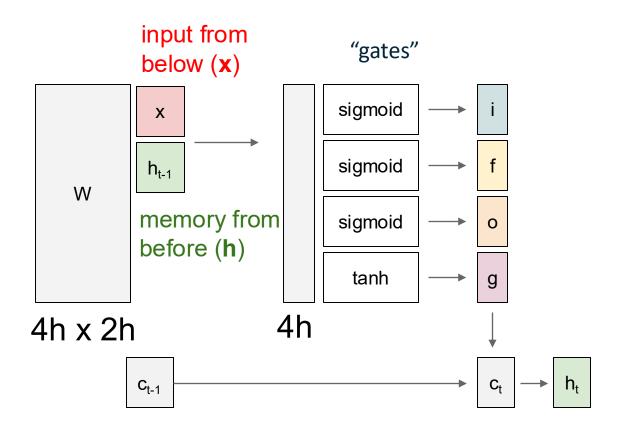
$$c_t = f_t \odot c_{t-1} + i_t \odot g_t$$
$$h_t = o_t \odot \tanh(c_t)$$

$$\frac{\partial c_t}{\partial c_{t-1}} = f_t + \frac{\partial i_t \odot g_t}{\partial c_{t-1}}$$
(forget gate)

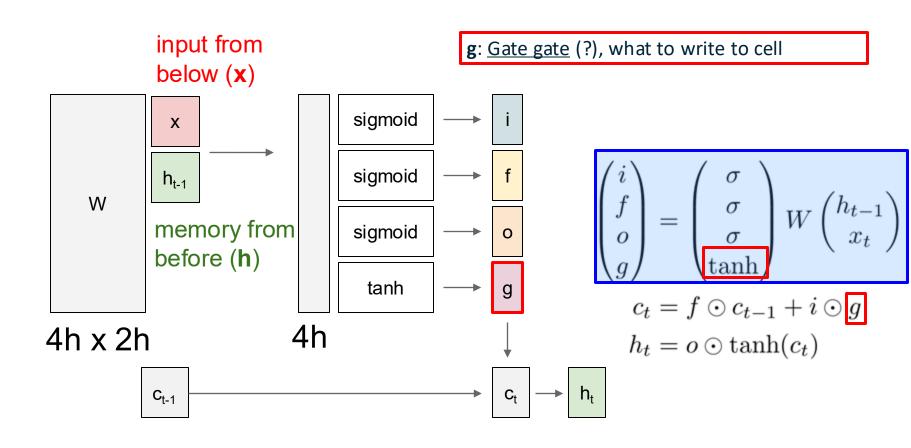
Different each step!

When  $f_t$  is close to 1, it allows gradient to flow back easily

[Hochreiter et al., 1997]

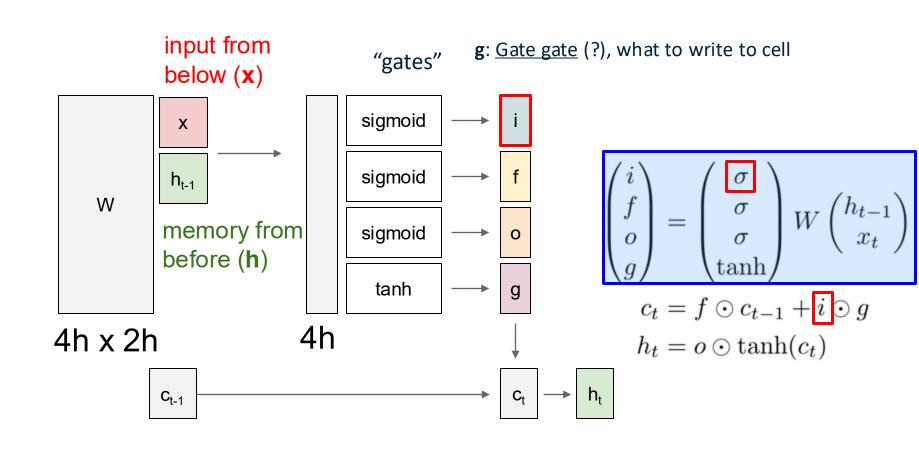


[Hochreiter et al., 1997]



[Hochreiter et al., 1997]

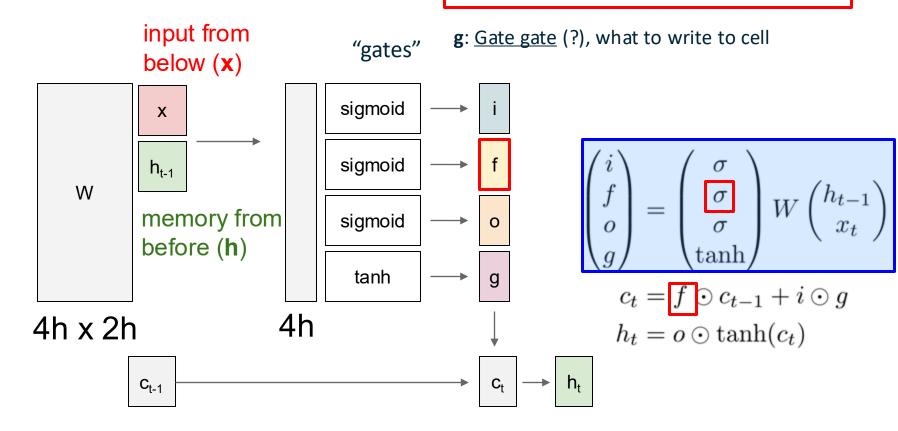
i: Input gate, whether to write to cell



[Hochreiter et al., 1997]

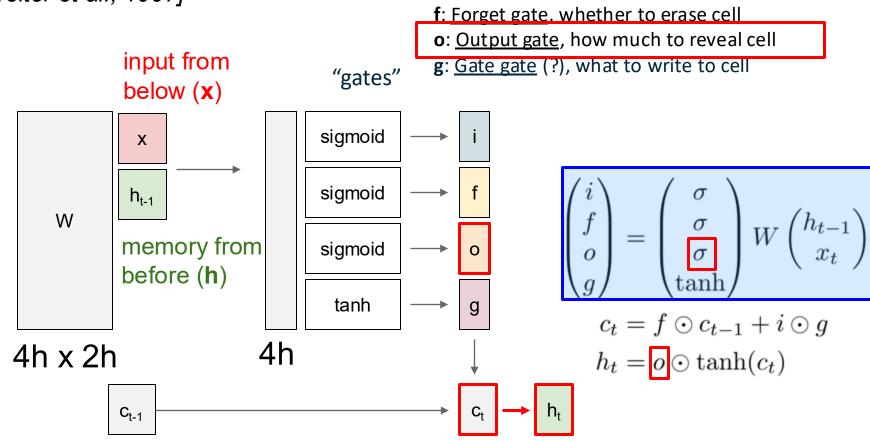
i: Input gate, whether to write to cell

f: Forget gate, whether to erase cell



[Hochreiter et al., 1997]

i: Input gate, whether to write to cell



# Do LSTMs solve the vanishing gradient problem?

The LSTM architecture makes it easier for the RNN to preserve information over many timesteps

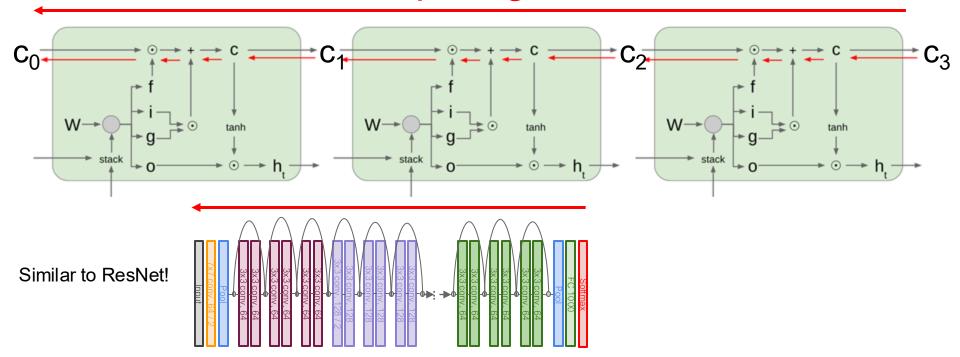
- e.g. if f = 1 and i = 0, then the information of that cell is preserved indefinitely. Gradient flow back from cell c easily.
- By contrast, it's harder for vanilla RNN to learn a recurrent weight matrix Wh that preserves info in hidden state

LSTM doesn't guarantee that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies.

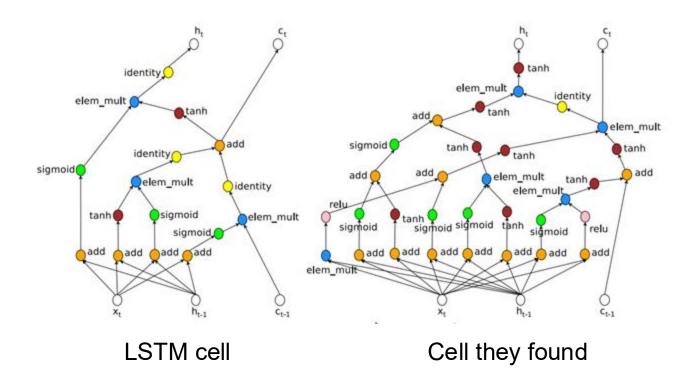
It is possible to mitigate vanishing / exploding gradient by learning the correct f

# Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

## Uninterrupted gradient flow!



#### Neural Architecture Search for RNN architectures



Zoph et Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Figures copyright Zoph et al, 2017. Reproduced with permission.

#### Other RNN Variants

**GRU** [Learning phrase representations using rnn encoder-decoder for statistical machine translation, Cho et al. 2014]

$$r_{t} = \sigma(W_{xr}x_{t} + W_{hr}h_{t-1} + b_{r})$$

$$z_{t} = \sigma(W_{xz}x_{t} + W_{hz}h_{t-1} + b_{z})$$

$$\tilde{h}_{t} = \tanh(W_{xh}x_{t} + W_{hh}(r_{t} \odot h_{t-1}) + b_{h})$$

$$h_{t} = z_{t} \odot h_{t-1} + (1 - z_{t}) \odot \tilde{h}_{t}$$

Simpler than LSTM, but control information flow without cell state.

[An Empirical Exploration of Recurrent Network Architectures, Jozefowicz et al., 2015]

#### MUT1:

$$\begin{array}{rcl} z &=& \operatorname{sigm}(W_{\operatorname{xz}}x_t + b_{\operatorname{z}}) \\ r &=& \operatorname{sigm}(W_{\operatorname{xr}}x_t + W_{\operatorname{hr}}h_t + b_{\operatorname{r}}) \\ h_{t+1} &=& \operatorname{tanh}(W_{\operatorname{hh}}(r\odot h_t) + \operatorname{tanh}(x_t) + b_{\operatorname{h}})\odot z \\ &+& h_t\odot(1-z) \end{array}$$

#### MUT2:

$$\begin{array}{rcl} z &=& \mathrm{sigm}(W_{\mathrm{xz}}x_t + W_{\mathrm{hz}}h_t + b_{\mathrm{z}}) \\ r &=& \mathrm{sigm}(x_t + W_{\mathrm{hr}}h_t + b_{\mathrm{r}}) \\ h_{t+1} &=& \mathrm{tanh}(W_{\mathrm{hh}}(r\odot h_t) + W_{xh}x_t + b_{\mathrm{h}})\odot z \\ &+& h_t\odot (1-z) \end{array}$$

#### MUT3:

$$z = \operatorname{sigm}(W_{xz}x_t + W_{hz} \tanh(h_t) + b_z)$$

$$r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

[LSTM: A Search Space Odyssey, Greff et al., 2015]

### Recommendations

- If you want to use RNN-like models, try LSTM
- Use variants like GRU if you want faster compute and less parameters
- New variants of RNNs are still active research topic. Example: RWKV ("Transformer-level performance but with RNN")

#### Problem with Recurrent-style Models (RNN, LSTM, GRU, etc.)

**Learning to memorize** is still hard, especially for ultra-long sequences!

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
 cell  $c$  can retain **important information** for **arbitrary future prediction problems**.   
 Example (Q&A): [... (20-page long transcript)]. Q: What did the CEO say about their competitor company? ... 
$$c_t = f \odot c_{t-1} + i \odot g$$
 [... (same 20-page transcript)]. Q: How many times did the journalist use the word "interesting"? ...

Essentially trying to tune W such that the memory cell c can retain **important information** for **arbitrary** future prediction problems.

say about their competitor company? ...

[... (same 20-page transcript)]. Q: How many times did the journalist use the word "interesting"? ...

Very difficult learning problem!

# Next time: Transformer Architecture

(What memory? Just show me the sequence again)